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## Previous Year Paper

Mathematics - 2013

## E Short Answer Type

1. If $(A-2 I)(A-3 I)=0$, where $A=42-1 x$ and $I=1001$, find the value of $x$.

Answer
2. Find the values of $k$ so that the line $2 x+y+k=0$ may touch the hyperbola $3 x^{2}-y^{2}=3$

Answer
3. Prove that: $\tan -114+\tan -129=12 \sin -145$

Answer
4. Using L'Hospital's Rule, evaluate:
$\lim x \rightarrow 0 e x-e-x-2 x x-\sin x$
Answer
5. Evaluate: $\int 1 x+x d x$

Answer
6. Evaluate: $\int 01 \log 1 x-1 d x$

Answer
7. Two regression lines are represented by $4 x+10 y=9$ and $6 x+3 y=4$. Find the line of regression of $y$ on $x$.

Answer
8. If $1, w$, and $w^{2}$ are the cube roots of unity, evaluate $\left(1-w^{4}+w^{8}\right)\left(1-w^{8}+w^{16}\right)$

Answer
9. Solve the differential equation:
logdydx $=2 x-3 y$
Answer
10. If two balls are drawn from a bag containing three red balls and four blue balls, find the probability that:
(a) They are of the same colour
(b) They are of different colours

Answer
11. Using properties of determinnats, prove that:
$x y z x 2 y 2 z 2 y+z z+x x+y=(x-y)(y-z)(z-x)(x+y+z)$
Answer

13. Corाstruct a circuit diayाamfor the following Boolean Function:

Using laws of Boolean Algebra, simplify the function and draw the simplified circuit.
Answer
14. Verify Lagrange's Mean value theorem for the function $f(x)=x 2-x$ in the interval [1, 4]. Answer
15. From the following information, find the equation of the Hyperbola and the equation of its Transverse Axis:

Focus: $(-2,1)$, Directrix: $2 x-3 y+1=0, e=23$
Answer
16. If $y=$ cot- $1 \times 2$, show that $1+x 2 d 2 y d x 2+2 x(1+x 2) d y d x=2$

Answer
17. Find the maximum value of the cylinder which can be inscribed in a sphere of radius 33 cm . (Leave the answer in terms of $\pi$ )

Answer
18. Evaluate: $\int \cos -1 x x 2 d x$

Answer
19. Find the area bounded by the curve $y=2 x-x^{2}$, and the line $y=x$

Answer
20. Find the Karl Pearson's co-efficient of correlation between $x$ and $y$ for the following data:

| $x$ | 16 | 18 | 21 | 20 | 22 | 26 | 27 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 22 | 25 | 24 | 26 | 25 | 30 | 33 | 14 |

Answer
21. The following table shows the mean and standard deviation of the marks of Mathematics and Physics scored by the students in a school:

|  | Mathematics | Physics |
| :---: | :---: | :---: |
| Mean | 84 | 81 |
| Standard Deviation | 7 | 4 |

The correlation coefficient between the given marks is 0.86 . Estimate the likely marks in physics if the marks in Mathematics are 92.
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Answer
23. Three persons Aman, Bipin and Mohan attempt a mathematics problem independently. The odds in favour of Aman and Mohan solving the problem are $3: 2$ and $4: 1$ respectively and the odds against Bipin solving the problem are 2:1. Find:
(i) The probability that all the three will solve the problem.
(ii) The probability that problem will be solved.

Answer
24. If the sum and the product of the mean and variance of a Binomial Distribution are 1.8 and 0.8 respectively, find the probability distribution the probability of at least one success.

Answer
25. The price index for the following data for the year 2011 taking 2001 as the base year was 127. The simple average price relatives method was used. Find the value of $x$ :

| Items | A | B | C | D | E | F |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Price (Rs. per <br> unit)in 2001 | 80 | 70 | 50 | 20 | 18 | 25 |
| Price (Rs. per <br> unit)in 2011 | 100 | $87-50$ | 61 | 22 | $X$ | 32.50 |

Answer
26. The profits of a paper bag manufacturing company (in laks of rupees) during each month of a year are :

| Month | Jan | Feb | Mar | Apr | May | June | July | Aug | Sept | Oct | NOV | Dec |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Profit | 1.2 | 0.8 | 1.4 | 1.6 | 2.0 | 2.4 | 3.6 | 4.8 | 3.4 | 1.8 | 0.8 | 1.2 |

Plot the given data on a graph sheet. Calculate the four monthly moving averages and plot these on the same graph sheet.

Answer

## 酋目 Long Answer Type

27. Find $A^{-1}$, where $A=42311131-2$

Hence, solve the following system of linear equations:
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Answer
28. Find the locus of the complex number $z=x+i y$, satisfying relations age $(z-1)=\pi 4$, and $z-2$ $3 i=2$. Illustrate the locus on the Argand plane.

Answer
29. Solve the following differential equation:
$y e^{y} d x=\left(y^{3}+2 x e^{y}\right) d y$, given that $x=0, y=1$.
Answer
30. Find the value of $\lambda$ for which the four points $A, B, C, D$ with position vectors - $\mathrm{j}^{\wedge}$ $\mathrm{k}^{\wedge} ; 4 \mathrm{i}^{\wedge}+5 \mathrm{j}^{\wedge}+\lambda \mathrm{k}^{\wedge} ; 3 \mathrm{i}^{\wedge}+9 \mathrm{j}^{\wedge}+4 \mathrm{k}^{\wedge}$ and $-4 \mathrm{i}^{\wedge}+4 \mathrm{j}^{\wedge}+4 \mathrm{k}^{\wedge}$ are coplanar.

Answer
31. If $a \rightarrow$ and $b \rightarrow$ are unit vectors and $\theta$ is the angle between them, then show that $a \rightarrow-$ $b \rightarrow=2 \sin (\theta 2)$

Answer
32. Find the equation of line passing through the point (-1, 3, - 2 ) and perpendicular to the lines: $x 1=y 2=z 3$ and $x+2-3=y-12=z+15$

Answer
33. Find the equations of planes parallel to the plane $2 x-4 y+4 z=7$ and which are at a distance of five units from the point $(3,-1,2)$ Answer
34. For $A, B$ and $C$, the chances of being selected as manager of a firm are $4: 1: 2$, repectively. The probabilities for them to introduce a radical change in the marketing strategy are $0.3,0.8$ and 0.5 respectively. If a change takes place; find the probability that it is due to the appontment of B.

Answer
35. Mr. Nirav deposits Rs. 250 at the beginning of each month in an account that pays an interest of 6 \% per annum compounded monthly, how many months will be required for the deposit to amount to at least Rs. 6390?

Answer
36. A mill owner buys two types of machines A and B for his mill. Machine A occupies 1000sqm of area and requires 12 men to operate it; while machine B occupies 1200 sqm of area and requires 8 men to operate it. The qwner has 7600 sqm of area available and 72 men to operate the machines. If machine A produces 50 units B produces 40 units daily, how many machines of each type should he buy to maximise the daily output? Use Linear Programming to find the solutions.
Answer



25 \% of the total revenue recovered on selling the product at a rate of Rs. 8 per unit. Find the following:
(i) Cost function
(ii) Revenue function
(iii) Breakeven point

Answer

