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Previous Year Paper

Mathematics - 2014

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Short Answer Type

1. If $A = 3175$, find the values of x and y such that $A^2 + xI_2 = yA$

[Answer](#)

2. Find the eccentricity and the coordinates of foci of the hyperbola $25x^2 - 9y^2 = 225$

[Answer](#)

3. Evaluate: $\tan 2 \tan 112^\circ - \cot 13^\circ$

[Answer](#)

4. Using L'Hospital's Rule, evaluate: $\lim_{x \rightarrow 0} 1 + x \cot x$

[Answer](#)

5. Evaluate: $\int e^x (2 + \sin 2x \cos 2x) dx$

[Answer](#)

6. Using properties of definite integrals, evaluate: $\int_0^{\pi/2} \sin x \sin x + \cos x dx$

[Answer](#)

7. For the given lines of regression, $3x - 2y = 5$, and $x - 4y = 7$, Find:

(i) regression coefficient b_{yx} and b_{xy}

(ii) coefficient of correlation $r(x, y)$

[Answer](#)

8. Express the complex number $1 + 3i\sqrt{3} - i$ in the form of $a + ib$. Hence, find the modulus and argument of the complex number.

[Answer](#)

9. A bag contains 20 balls numbered from 1 to 20. One ball is drawn at random from the bag. What is the probability that the ball drawn is marked with a number which is multiple of 3 or 4?

[Answer](#)

10. Solve the differential equation:

$$x + 1 dy - 2xy dx = 0$$

[Answer](#)

11. Using properties of determinants, prove that:

$$a^2 + 1abacbab^2 + 1bccacbc^2 + 1 = a^2 + b^2 + c^2 + 1$$

[Answer](#)

12. Using matrix method, solve the following system of equation:

$$x - 2y = 10, 2x + y + 3z = 8 \text{ and } -2y + z = 7,$$

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13. If $\cos^{-1}x + \cos^{-1}y + \cos^{-1}z = \pi$, prove that: $x^2 + y^2 + z^2 + 2xyz = 1$
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Answer

14. P, Q and R represent switches in on position and P', Q' and R' represent switches in off position. Construct a switching circuit representing the polynomial $PR + Q(Q' + R)(P + QR)$. Using Boolean algebra, simplify the polynomial expression and construct the simplified circuit.

Answer

15. Verify Rolle's theorem for the function $f(x) = e^x \sin x - \cos x$ on $\pi/4, 5\pi/4$

Answer

16. Find the equation of the parabola with latus-rectum joining points (4, 6) and (4, -2).

Answer

17. If $y = x \sin^{-1}x - x^2$, prove that: $1 - x^2 dy/dx = x + yx$

Answer

18. A wire of length 50m is cut into two pieces. One piece of the wire is bent in the shape of a square and the other in the shape of a circle. What should be the length of each piece so that the combined area of the two is minimum.

Answer

19. Evaluate: $\int x + \sin x + \cos x dx$

Answer

20. Sketch the graphs of the curve $y^2 = x$ and $y^2 = 4 - 3x$ and find the area enclosed between them.

Answer

21. A psychologist selected a random sample of 22 students. He grouped them in 11 pairs so that the students in each pair have nearly equal scores in an intelligence test. In each pair, one student was taught by method A and the other by method B and examined after the course. The marks obtained by them after the course are as follows:

Pairs	1	2	3	4	5	6	7	8	9	10	11
Method A	24	29	19	14	30	19	27	30	20	28	11
Method B	37	35	16	26	23	27	19	20	16	11	21

Calculate Sperman's Rank correlation.

Answer

22. In a college, 70% students pass in physics, 75% pass in Mathematics and 105 students fail in both. One student is chosen at random. What is the probability that:

- (i) He passes in Physics and Mathematics.
(ii) He passes in Mathematics given that he passes in Physics.
(iii) He passes in Physics given that he passes in Mathematics.

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Answer

23. A bag contains 1 white and 4 black balls and another bag contains 7 white and 2 black balls. A ball is drawn from the first bag and two balls are drawn from the second bag. What is the probability of drawing one white and two black balls ?

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[Answer](#)

24. Using De Moivre's theorem, find the least positive integer n such that $2i^{1+n}$ is a positive integer.

[Answer](#)

25. Prove that: $a \rightarrow (b \rightarrow c) \times a \rightarrow + 2b \rightarrow + 3c \rightarrow = a \rightarrow b \rightarrow c \rightarrow$

[Answer](#)

26. Find the equation of a line passing through the points $P(-1, 3, 2)$ and $Q(-4, 2, -2)$. Also, if the points $R(5, 5, \lambda)$ is collinear with the points P and Q , then find the value of λ .

[Answer](#)

27. Find the equation of the plane passing through the points $(2, -3, 1)$ and $(-1, 1, -7)$ and perpendicular to the plane $x - 2y + 5z + 1 = 0$

[Answer](#)

28. In a bolt factory, three machines A , B and C manufacture 25 %, 35 %, and 40 % of the total production respectively. Of their respective outputs, 5 %, 4 % and 2 % are defective. A bolt is drawn at random from the total production and it is found to be defective. Find the probability that it was manufactured by machine C .

[Answer](#)

29. On dialing certain telephone numbers, assume that on an average, one telephone number out of five is busy. ten telephone numbers are randomly selected and dialed. Find the probability that at least three of them will be busy.

[Answer](#)



Long Answer Type

30. The coefficient of correlation between the values denoted by X and Y is 0.5. The mean of X is 3 and that of Y is 5. Their standard deviations are 5 and 4 respectively. Find:
- the two lines of regression
 - the expected value of Y , when X is given 14.
 - the expected value of X , when Y is given 9.

[Answer](#)

31. Solve the following differential equation.

$$3xy + y^2 dx + x^2 + xy dy = 0$$

[Answer](#)

32. In a triangle ABC , using vectors, prove that $c^2 = a^2 + b^2 - 2ab \cos(C)$

[Answer](#)

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33. A person borrows 68,962 on the condition that he will repay the money with compound interest at 5 % per annum, installments, the first one being payable at the end of the first year. Find the value of each installment.

Answer

34. A company manufactures two types of toys A and B. a toy of type A requires 5 minutes for cutting and 10 minutes for assembling. A toy of type B requires 8 minutes for cutting and 8 minutes for assembling. There are 3 hours available for cutting and 4 hours available for assembling the toys in a day. The profit is 50 each on a toy of type A and 60 each on a toy of type B.. How many toys of each type should the company manufacture in a day to maximize the profit? Use linear programming to find the solution.

Answer

35. The price of six different commodities for years 2009 and year 2011 are as follows:

Commodities	A	B	C	D	E	F
Price in 2009()	35	80	25	30	80	x
Price in 2011()	50	y	45	70	120	105

The index number for the year 2011 taking 2009 as the base year for the above data was calculated to be 125.. Find the values of x and y if the total price in 2009 is 360.

Answer

36. The number of road accidents in the city due to rash driving, over a period of 3 years, is given in the following table:

Year	Jan - Mar	April - June	July - Sept.	Oct. - Dec.
2010	70	60	45	72
2011	79	56	46	84
2012	90	64	45	82

Calculate four quarterly moving averages and illustrate them and original figures on one graph using the same axes for both.

Answer

37. A firm has the cost function $C = x^3 - 7x^2 + 11x + 50$ and demand function $x = 100 - p$
- Write the total revenue function in terms of x.
 - Formulate the total profit function P in terms of x.
 - Find the profit maximising level of output x.

Answer

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38. A bill of Rs. 9000 is drawn on 13th April 2013. It was discounted on 4th July 2013 at 5 % per annum. If the banker's gain on the transaction is Rs. 0.50, find the nominal date of the maturity of the bill.

[Answer](#)